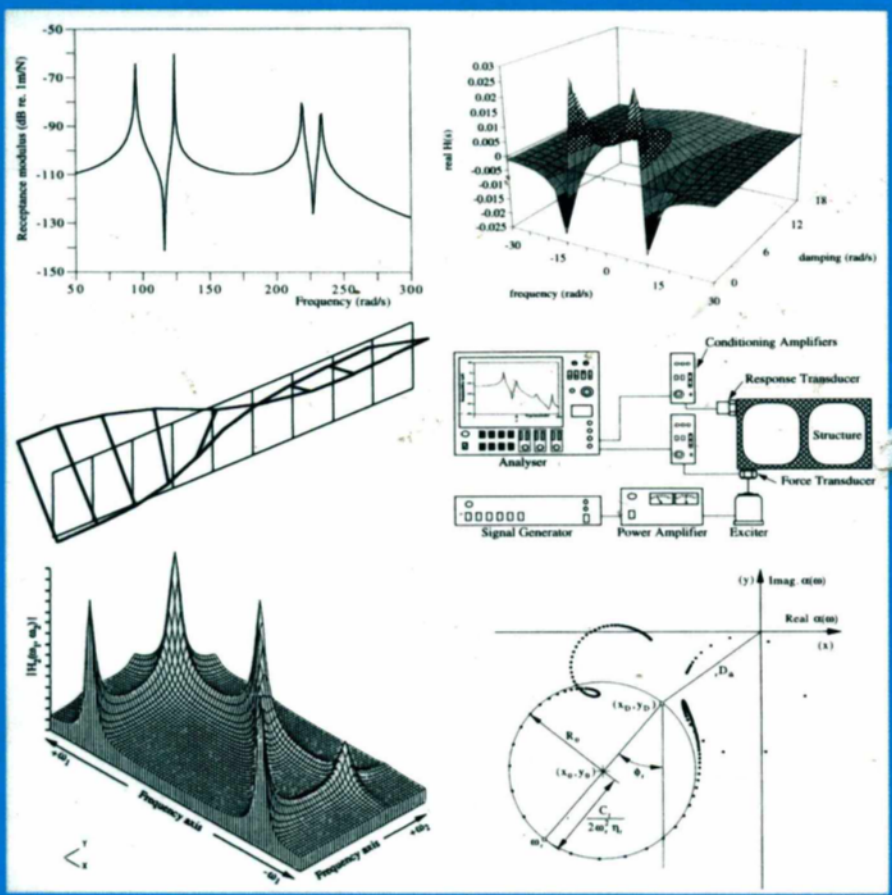
Theoretical and Experimental Modal Analysis

Maia, Silva,
He, Lieven, Lin, Skingle, To, Urgueira



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Contributing Authors

Nuno Manuel Mendes Maia
Associate Professor
Department of Mechanical Engineering
Instituto Superior Técnico / Technical University of Lisbon, Lisbon, Portugal

Júlio Martins Montalvão e Silva
Professor
Department of Mechanical Engineering
Instituto Superior Técnico / Technical University of Lisbon, Lisbon, Portugal

Jimin He
Senior Lecturer
Department of Mechanical Engineering
Victoria University of Technology, Melbourne, Australia

Nicholas Andrew John Lieven
Lecturer
Department of Aerospace Engineering
University of Bristol, Bristol, United Kingdom

Rong Ming Lin
Lecturer
School of Mechanical and Production Engineering
Nanyang Technological University, Singapore, Republic of Singapore

Graham William Skingle
Research Scientist
Aero-Structures Department
Defence Evaluation and Research Agency, Farnborough, United Kingdom

Wai-Ming To
Assistant Professor
Mechanical Engineering Department
The Hong Kong University of Science & Technology, Kowloon, Hong-Kong

António Paulo Vale Urgueira
Associate Professor
Department of Mechanical Engineering
Faculty of Sciences and Technology / New University of Lisbon, Monte da Caparica, Portugal

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